

5/15  
 \* 51.  $\cos^4 x - \sin^4 x = 1 - 2\sin^2 x$   
 $(\cos^2 x + \sin^2 x)(\cos^2 x - \sin^2 x)$   
 $(\cos^2 x - \sin^2 x)$   
 $\frac{1 - \sin^2 x - \sin^2 x}{1 - 2\sin^2 x} = 1 - 2\sin^2 x$

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!!  
 $\frac{\csc \theta - \sin \theta}{\sin \theta} = \cot \theta \cos \theta$   
 $\frac{1 - \sin^2 \theta}{\sin \theta} = \frac{\cos^2 \theta}{\sin \theta}$   
 $\frac{\cos \theta \cdot \cos \theta}{\sin \theta} = \cot \theta \cos \theta$

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Solving Trig & QS Notes  
 1).  $3\sin x - 2 = 5\sin x - 1$   
 like  $3x - 2 = 5x - 1$   
 $\frac{-2\sin x - 1}{-2} = \frac{1}{-2}$   
 $\sin x = -\frac{1}{2}$   
 Solving over  $0 \leq \theta < 2\pi$   
 $\frac{\pi}{6}$  fam

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b)  $5\sin x = 3\sin x + \sqrt{3}$   
 like  $5x = 3x + \sqrt{3}$   
 $2\sin x = \sqrt{3}$   
 $\sin x = \frac{\sqrt{3}}{2}$   
 $x = \frac{\pi}{3}, \frac{2\pi}{3}$   
 $\frac{\pi}{3} (\frac{1}{2}, \frac{\sqrt{3}}{2})$   
 $\sin x = \frac{\sqrt{3}}{2}$

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#2  $\pm \sqrt{\quad}$   
 $(\quad)^2 \pm \text{constant} = 0$   
 $4\sin^2 x + 5 = 6$  no "linear" term  
 like  $4x^2 + 5 = 6$  no plain x term.  
 $4x^2 = 1$   
 $\sin^2 x = \frac{1}{4}$   
 $\sin x = \pm \sqrt{\frac{1}{4}}$   $\sin x = \pm \frac{1}{2}$   
 $\frac{\pi}{6}$  fam.  
 $\frac{5\pi}{6}, \frac{7\pi}{6}, \frac{11\pi}{6}$

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b.  $3\sec^2 x - 4 = 0$   $3x^2 - 4 = 0$   
 $\sec^2 x = \frac{4}{3}$   $3x^2 = 4$   
 $\sec x = \pm \sqrt{\frac{4}{3}}$   $x^2 = \frac{4}{3}$   
 $\sec x = \pm \frac{2}{\sqrt{3}}$   $x = \pm \sqrt{\frac{4}{3}}$   
 reciprocal of  $\cos x$   $\frac{1}{\cos x} = \pm \frac{2}{\sqrt{3}}$   
 $\cos x = \pm \frac{\sqrt{3}}{2}$   $\sec x = \pm \frac{2}{\sqrt{3}}$   
 $\frac{5\pi}{6}, \frac{7\pi}{6}, \frac{11\pi}{6}, \frac{13\pi}{6}$   $\frac{\pi}{6}$  fam.

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③  $\tan(3x) = 1$   
 Let  $k = 3x$   
 $\therefore \tan k = 1$   
 $k = \frac{\pi}{4}$      $k = \frac{5\pi}{4}$   
 $\frac{1}{3}3x = \frac{\pi}{4} \cdot \frac{1}{3}$      $3x = \frac{5\pi}{4}$   
 $x = \pi/12$      $x = 5\pi/12$

$\tan = \frac{y}{x}$   
 $\frac{y}{x} = 1$

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$\sec(4x) = 2$   
 let  $k = 4x$   
 $\therefore \sec k = 2$   
 $\frac{1}{\cos k} = \frac{2}{1}$   
 $\cos k = \frac{1}{2}$

replace  $\sec x$  with  $\frac{1}{\cos x}$

$k = \frac{\pi}{3}$      $k = \frac{5\pi}{3}$   
 $4x = \frac{\pi}{3}$      $4x = \frac{5\pi}{3}$   
 $x = \frac{\pi}{12}$      $x = \frac{5\pi}{12}$

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e).  $\sin \frac{x}{2} = \frac{\sqrt{3}}{2}$   
 let  $k = \frac{x}{2}$   
 $\sin k = \frac{\sqrt{3}}{2}$

$k = \frac{\pi}{3}$      $k = \frac{2\pi}{3}$   
 $\frac{x}{2} = \frac{\pi}{3}$      $\frac{x}{2} = \frac{2\pi}{3}$   
 $x = \frac{2\pi}{3}$      $x = \frac{4\pi}{3}$

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S4. g)  $2\cos^2 x + \cos x - 1 = 0$   
 que  $(2x^2 + x - 1 = 0)$   
 let  $u = \cos x$ :  $2u^2 + u - 1 = 0$   
 $(2u - 1)(u + 1) = 0$   
 $2u - 1 = 0$      $u + 1 = 0$   
 $u = \frac{1}{2}$      $u = -1$   
 $\cos x = \frac{1}{2}$      $\cos x = -1$

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$2\sin^2 x - 3\sin x + 1 = 0$   
 let  $u = \sin x$   
 $2u^2 - 3u + 1 = 0$   
 $(2u - 1)(u - 1) = 0$   
 $2u - 1 = 0$      $u - 1 = 0$   
 $u = \frac{1}{2}$      $u = 1$   
 $\sin x = \frac{1}{2}$      $\sin x = 1$

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#5. GCF  
 1).  $\tan x \sin^2 x = 3 \tan x$   
 $\tan x \sin^2 x - 3 \tan x = 0$   
 $\tan x (\sin^2 x - 3) = 0$   
 $\tan x = 0$      $\sin^2 x - 3 = 0$   
 $\sin^2 x = 3$   
 $\sin x = \pm \sqrt{3}$   
 $\sin x = \pm 1.73$

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j.  $\sin x \tan x = \sin x$   
DO NOT DIVIDE  
 $\sin x \tan x - \sin x = 0$   
 $\sin x (\tan x - 1) = 0$   
 $\sin x = 0$        $\tan x - 1 = 0$   
 $\tan x = 1$

$0, \pi, \frac{\pi}{4}, \frac{5\pi}{4}$

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S6  $2 \cos^2 x + 3 \sin x = 0$   
 replace with  $1 - \sin^2 x$   
 to create an eq. in one trig fn.  
 $2(1 - \sin^2 x) + 3 \sin x = 0$   
 $2 - 2 \sin^2 x + 3 \sin x = 0$   
 $-2 \sin^2 x + 3 \sin x + 2 = 0$   
 $2 \sin^2 x - 3 \sin x - 2 = 0$   
 $(2 \sin x + 1)(\sin x - 2) = 0$   
 OR let  $u = \sin x$   
 $2u^2 - 3u - 2 = 0$   
 $(2u + 1)(u - 2) = 0$   
 $\sin x = -\frac{1}{2}$        $\sin x = 2$   
 $2u + 1 = 0$        $u - 2 = 0$   
 $2 \sin x = -1$        $u = 2$   
 $\sin x = -\frac{1}{2}$        $\sin x = 2$

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