

Int. Algebra Review - Solving Quadratics

Key

Name _____

I. Solve by Factoring

Perfect Trinomial Square

1.) $3x^2 - 2x - 16 = 0$

$$(3x - 8)(x + 2) = 0$$

$\begin{array}{r} \text{---} \\ -8x \\ \text{---} \\ +6x \\ \text{---} \end{array}$

$x = \frac{8}{3}$ $x = -2$

2.) $4x^2 - 20x + 25 = 0$

$$(2x - 5)(2x - 5) = 0$$

$x = \frac{5}{2}$

3.) $x^2 + 3x = 40$

$$x^2 + 3x - 40 = 0$$

$$(x + 8)(x - 5) = 0$$

$x = -8$
 $x = 5$

4.) $2x^2 = 15x - 27$

$$2x^2 - 15x + 27 = 0$$

$$(2x + 3)(x - 9) = 0$$

$x = -\frac{3}{2}$ $x = 9$

5.) $9x^2 - 100 = 0$

$$(3x + 10)(3x - 10) = 0$$

$x = -\frac{10}{3}$
 $x = \frac{10}{3}$

6.) $x^2 + 6x = 0$

$$x(x + 6) = 0$$

$x = 0$
 $x = -6$

II. Solve by Square Roots. Express your solutions in simplest radical form. You must always use _____ when solving using square roots.

7.) $x^2 = 80$

$$x = \pm \sqrt{80}$$

$$x = \pm \sqrt{4 \cdot 20}$$

$$x = \pm 2 \sqrt{4 \cdot 5}$$

$$x = \pm 4\sqrt{5}$$

8.) $4x^2 = 81$

$$x^2 = \frac{81}{4}$$

$$x = \pm \frac{9}{2}$$

9.) $x^2 + 7 = -300$

$$x^2 = -307$$

$$x = \pm \sqrt{-307}$$

no real solution

10.) $(x - 5)^2 = 36$

$$x - 5 = \pm \sqrt{36}$$

$$x - 5 = \pm 6$$

$$x = 5 \pm 6$$

$$x = 5 + 6$$

$$= 11$$

$$x = 5 - 6$$

$$= -1$$

11. $5(x + 2)^2 - 4 = 36$

III. Solve by using the quadratic formula.

The quadratic formula is: $x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$

Given $0 = ax^2 + bx + c$

12. $x^2 + 3x + 5 = 0$

$a = 1$

$b = 3$

$c = 5$

$b^2 - 4ac = 9 - 4(1)(5)$
 $= -11$

$\sqrt{b^2 - 4ac} = \sqrt{-11}$

no real solution

13. $4x^2 - 8x = 1$

$4x^2 - 8x - 1 = 0$

$a = 4$

$b = -8$

$c = -1$

$b^2 - 4ac$
 $= (-8)^2 - 4(4)(-1)$
 $= 64 + 16$
 $= 80$

$\sqrt{b^2 - 4ac} = \sqrt{80} = \sqrt{4 \cdot 20}$
 $= 2\sqrt{20}$
 $= 2 \cdot 2\sqrt{5} = 4\sqrt{5}$

14. $x^2 + 8x = 8$

$x^2 + 8x - 8 = 0$

$a = 1$ $b = 8$ $c = -8$

$b^2 - 4ac = (8)^2 - 4(1)(-8)$
 $= 64 + 32 = 96$
 $\sqrt{b^2 - 4ac} = \sqrt{96} = \sqrt{16 \cdot 6}$
 $= 4\sqrt{6}$

$x = \frac{-8 \pm 4\sqrt{6}}{2} = \frac{-4 \pm 2\sqrt{6}}{1}$

$x = \frac{8 \pm 4\sqrt{5}}{8}$

$x = \frac{2 \pm \sqrt{5}}{2}$

15) What are the two mistakes in setting up the quadratic formula? Find them and fix them!

Solve: $2x^2 - x - 6 = 0$

$a = 2$

$b = -1$

$c = -6$

should be \leftarrow should be -6
 The opp. of -1 which is 1.

$x = \frac{-1 \pm \sqrt{(-1)^2 - 4(2)(6)}}{2(2)}$

$x = \frac{1 \pm \sqrt{(-1)^2 - 4(2)(-6)}}{4}$

$x = \frac{1 \pm \sqrt{1 + 48}}{4}$

$x = \frac{1 \pm \sqrt{49}}{4}$

$x = \frac{1 \pm 7}{4} \rightarrow \frac{1+7}{4} = \frac{8}{4} = 2$

$\frac{1-7}{4} = \frac{-6}{4} = \frac{-3}{2}$

IV. REVIEW – PROJECTILE MOTION PROBLEMS

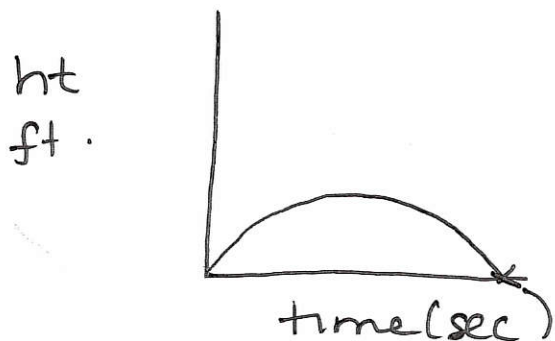
Projectile Motion Formula: $h(t) = -16t^2 + V_0t + h_0$

where: $h(t)$ is ending time after t seconds, $V_0 =$ initial velocity, $h_0 =$ initial height.
 GROUND means that the ending height after t seconds is \bigcirc .

1. Julia kicks soccer ball from the ground with an initial velocity of 32 feet per second.

A. Write the equation that represents this situation. $h(t) = -16t^2 + 32t + 0$

B. Sketch and label the graph that represents this problem.



C. How many seconds will it take for the ball to hit the ground? Ground \rightarrow
set $h(t) = 0$.

$$0 = \frac{-16t^2}{-16} + \frac{32t}{-16}$$

$$0 = t^2 - 2t \quad \text{USE GCF}$$

$$t(t-2) = 0$$

$$t = 0 \quad t - 2 = 0$$

$$t = 2$$

2 secs.

D. How high will the ball be after 1 second?

$$16 \text{ ft.}$$

$$h(1) = -16(1)^2 + 32(1)$$

$$t = 16 \text{ ft.}$$

E. WHEN will the ball reach its maximum height? (Either use the roots or the formula $t = -b/2a$)

$$t = \frac{-b}{2a} = \frac{-32}{2(-16)} = 1 \text{ second.}$$

F. What is the maximum height that the ball reaches?

Sub in t max for time:

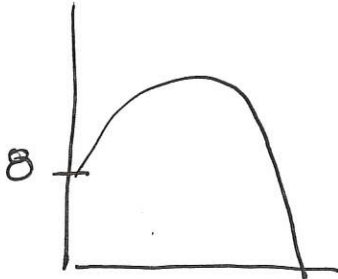
$$h(1) = -16(1)^2 + 32(1)$$

$$= 16 \text{ ft.}$$

2. Ray launches a rocket from a point 8 feet above the water with an initial upward velocity of 16 feet per second.

A. Write the equation that represents the problem. $h(t) = -16t^2 + 16t + 8$

B. Sketch and label a graph to represent the problem.



C. How long will it take the rocket to reach the water?

$$0 = \frac{-16t^2}{-8} + \frac{16t}{-8} + \frac{8}{-8}$$

$$0 = 2t^2 - 2t - 1$$

It doesn't factor! \therefore

$$h(t) = 0$$

Use QF

$$a = 2 \quad b = -2 \quad c = -1$$

$$b^2 - 4ac$$

$$= 4 - 4(2)(-1)$$

$$= 4 + 8 = 12$$

$$\sqrt{b^2 - 4ac} = \sqrt{12} = 2\sqrt{3}$$

$$x = \frac{2 \pm 2\sqrt{3}}{4} = \frac{1 \pm \sqrt{3}}{2}$$

D. How high will the rocket be after 1 second?

$$h(1) = -16(1)^2 + 16(1) + 8$$

$$-16 + 16 + 8 = 8 \text{ feet}$$

The equation $t = -b/2a$ can be used to find when the rocket will reach its maximum height.

Use it to find when the rocket will reach its max height.

$$t = \frac{-b}{2a} = \frac{-16}{-32} = \frac{1}{2}$$

E. What will its maximum height be?

Sub in $\frac{1}{2}$ for t

$$h\left(\frac{1}{2}\right) = -16\left(\frac{1}{2}\right)^2 + 16\left(\frac{1}{2}\right) + 8$$

$$= -4 + 8 + 8 = \textcircled{12 \text{ feet}}$$

Solving Quadratics REVIEW**I. Zero Product Property:**

If the product of two quantities equals zero, at least one of the quantities equals zero.

If $ab = 0$, then $a = 0$ or $b = 0$.

1. Use the Zero Product Property to solve the equation. Check your answers.

1. $(x-3)(x+7) = 0$

$x-3 = 0 \quad x+7 = 0$

$x = 3 \quad x = -7$

2. $x(x-5) = 0$

$x = 0 \quad x-5 = 0$

$x = 5$

3. $(3x+2)(4x-1) = 0$

$3x+2 = 0 \quad 4x-1 = 0$

$x = -2/3 \quad x = 1/4$

4. $2(4x-2)(2x+4) = 0$

$4x-2 = 0 \quad 2x+4 = 0$

$4x = 2 \quad 2x = -4$

$x = \frac{2}{4} \quad x = -2$

$x = \frac{1}{2}$

II.. Solve by Factoring

Objective: *I CAN* . . . solve quadratic equations by factoring.

Factor. Don't forget to check to see if there is a GCF first!

5. $x^2 + 10x + 16$

$(x-8)(x-2) = 0$

$x-8 = 0 \quad x-2 = 0$

$x = 8 \quad x = 2$

6. $x^3 + 2x^2 - 24x$

$x(x^2 + 2x - 24)$

$x(x+6)(x-4)$

7. $36x^2 - 49$

$(6x+7)(6x-7)$

III. Solve each by factoring and then using the zero product property. Always check for a GCF first!

1. $4x^2 + 21x + 5 = 0$

$$(4x + 1)(x + 5) = 0$$

$$4x + 1 = 0 \quad x + 5 = 0$$

$$4x = -1 \quad x = -5$$

$$x = -\frac{1}{4}$$

3. $3t^2 - 6t = 30$ (GCF!)

$$3t^2 - 6t - 30 = 0$$

$$3(t^2 - 2t - 10) = 0$$

~~3~~t can't factor

2. $x^2 - 8x + 12 = 0$

$$(x - 6)(x - 2) = 0$$

$$x = 6 \quad x = 2$$

4. $d^3 + d^2 - 20d = 0$ (GCF)

$$d(d^2 + d - 20) = 0$$

$$d(d + 5)(d - 4) = 0$$

$$d = 0 \quad d = 0$$

$$d + 5 = 0 \quad d = -5$$

$$d - 4 = 0 \quad d = 4$$

5. $25x^2 - 16 = 0$

$$(5x + 4)(5x - 4) = 0$$

$$5x + 4 = 0 \quad 5x - 4 = 0$$

$$x = -\frac{4}{5} \quad x = \frac{4}{5}$$

6. $25x^2 = 20x - 4$

$$25x^2 - 20x + 4 = 0$$

$$(5x - 2)(5x - 2) = 0$$

$$5x - 2 = 0 \quad 5x - 2 = 0$$

$$x = \frac{2}{5}$$

7. $4x^2 - 8x + 3 = 0$

$$(2x - 1)(2x - 3) = 0$$

$$2x - 1 = 0 \quad 2x - 3 = 0$$

$$2x = 1 \quad 2x = 3$$

$$x = \frac{1}{2} \quad x = \frac{3}{2}$$

IV. Solving with Square Roots

Objective: I CAN ... solve quadratic equations by using square roots.

Simplify completely.

1. $\sqrt{16} = 4$

2. $\sqrt{28} = \sqrt{4} \sqrt{7}$
 $= 2\sqrt{7}$

3. $\sqrt{75}$
 $= \sqrt{25} \sqrt{3}$
 $= 5\sqrt{3}$

4. $2\sqrt{60}$
 $2\sqrt{4} \sqrt{15}$
 $4\sqrt{15}$

5. $\frac{1}{3}\sqrt{9}$
 $\frac{1}{3} \cdot 3 = 1$

6. $\frac{1}{8}\sqrt{20}$
 $\frac{1}{8} \cdot \sqrt{4} \cdot \sqrt{5}$
 $\frac{1}{8} \cdot 2\sqrt{5}$
 $\frac{2\sqrt{5}}{8} = \frac{\sqrt{5}}{4}$

Solve for x.

1. $x^2 = 25$ $x = \pm 5$

If $x^2 = a$ and a is a positive real number then $x = \pm\sqrt{a}$

Solve using square roots.

1. $2x^2 = 16$

$x^2 = 8$
 $x = \pm\sqrt{8}$
 $x = \pm\sqrt{4} \sqrt{2}$
 $x = \pm 2\sqrt{2}$

2. $x^2 = -4$

$x = \pm\sqrt{-4}$
no real solutions.

3. $3x^2 - 81 = 0$

$3x^2 = 81$
 $x^2 = 27$
 $x = \pm\sqrt{27}$
 $x = \pm\sqrt{9} \sqrt{3}$
 $x = \pm 3\sqrt{3}$

4. $(x+2)^2 = 9$

$x+2 = \pm\sqrt{9}$
 $x = -2 \pm\sqrt{9}$
 $x = -2 \pm 3$

$\rightarrow -2+3=1$
 $\rightarrow -2-3=-5$

5. $3(x-2)^2 - 7 = 23$

$+7 \quad +7$

$\frac{3(x-2)^2}{3} = \frac{30}{3}$

$(x-2)^2 = 10$
 $x-2 = \pm\sqrt{10}$
 $x = 2 \pm\sqrt{10}$

V. Quadratic Formula

Objective: I CAN... solve by using the Quadratic Formula.

The Quadratic Formula:

The solutions of $ax^2 + bx + c = 0$ where $a \neq 0$ are $x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$

The discriminant of the quadratic equation is $b^2 - 4ac$.

Solve using the Quadratic Formula.

1. $2x^2 - 2x - 3 = 0$

$$a = 2 \quad b = -2 \quad c = -3$$

$$\begin{aligned} b^2 - 4ac &= (-2)^2 - 4(2)(-3) \\ &= 4 + 24 \\ &= 28 \end{aligned}$$

$$\sqrt{b^2 - 4ac} = \sqrt{28} = \sqrt{4 \cdot 7} = 2\sqrt{7}$$

$$\begin{aligned} x &= \frac{-b \pm 2\sqrt{7}}{4} = \frac{2 \pm 2\sqrt{7}}{4} \\ &= \frac{1 \pm \sqrt{7}}{2} \end{aligned}$$

3. $x^2 - 2x = 4$

$$x^2 - 2x - 4 = 0$$

$$a = 1$$

$$b = -2$$

$$c = -4$$

$$\begin{aligned} b^2 - 4ac &= (-2)^2 - 4(1)(-4) \\ &= 4 + 16 = 20 \end{aligned}$$

$$x = \frac{2 \pm \sqrt{20}}{2} = \frac{2 \pm 2\sqrt{5}}{2} = 1 \pm \sqrt{5}$$

2. $2x^2 + 3x + 5 = 0$

$$a = 2 \quad b = 3 \quad c = 5$$

$$\begin{aligned} b^2 - 4ac &= \\ (3)^2 - 4(2)(5) \\ 9 - 40 &= -31 \end{aligned}$$

$$\sqrt{-31} \rightarrow$$

no
real
solution.

4. $2x^2 = 8x - 1$

$$2x^2 - 8x + 1 = 0$$

$$a = 2$$

$$b = -8$$

$$c = 1$$

$$\begin{aligned} b^2 - 4ac &= (-8)^2 - 4(2)(1) \\ &= 64 - 8 \end{aligned}$$

$$b^2 - 4ac = 56$$

$$\begin{aligned} \sqrt{b^2 - 4ac} &= \sqrt{56} \\ &= \sqrt{4 \cdot 14} \\ &= 2\sqrt{14} \end{aligned}$$

$$\text{so } x = \frac{8 \pm 2\sqrt{14}}{4} = \frac{4 \pm \sqrt{14}}{2}$$