

Quadratic Formula Word Problems

Name: Key
 Date: _____
 Period: _____

1. Jason jumped off of a cliff into the ocean in Acapulco while vacationing with some friends. His height as a function of time could be modeled by the function $h(t) = -16t^2 + 16t + 480$, where t is the time in seconds and h is the height in feet.

a. How long did it take for Jason to reach his maximum height?

5 seconds

b. What was the highest point that Jason reached?

484 ft.

c. Jason hit the water after how many seconds?

6 seconds

2. If a toy rocket is launched vertically upward from ground level with an initial velocity of 128 feet per second, then its height h after t seconds is given by the equation $h(t) = -16t^2 + 128t$ (if air resistance is neglected).

a. How long will it take for the rocket to return to the ground?

8 seconds

b. After how many seconds will the rocket be 112 feet above the ground?

$t = 1 \text{ sec}$

$t = 7 \text{ sec}$

c. How long will it take the rocket to hit its maximum height?

4 sec

d. What is the maximum height?

256 ft.

-16t²

6. A diver is standing on a platform 24 ft. above the pool. He jumps from the platform with an initial upward velocity of 8 ft/s. Use the formula $h(t) = -16t^2 + vt + s$, where h is his height above the water, t is the time, v is his starting upward velocity, and s is his starting height. How long will it take for him to hit the water?

5. You are trying to dunk a basketball. You need to jump 2.5 ft. in the air to dunk the ball. The height that your feet are above the ground is given by the function $h(t) = -16t^2 + 12t$. What is the maximum height your feet will be above the ground? Will you be able to dunk the basketball?

$$a = -16$$

$$b = -32$$

$$x = \frac{-b}{2a} = \frac{+32}{-32} = -1 \text{ sec}$$

$$h(1) = -16 - 32 + 5$$

X You and a friend are hiking in the mountains. You want to climb to a ledge that is 20 ft. above you. The height of the grappling hook you throw is given by the function $h(t) = -16t^2 - 32t + 5$. What is the maximum height of the grappling hook? Can you throw it high enough to reach the ledge?

$$a = -16$$

$$b = 116$$

$$c = 101$$

$$x = \frac{-b}{2a} = \frac{-116}{-32} = 3.625$$

8 sec

$$h(3.625) = -16(3.625)^2 + 116(3.625) + 101$$

$$= -207.5 + 422.5 + 101 = 316$$

3. A rocket is launched from atop a 101-foot cliff with an initial velocity of 116 ft/s. a. Substitute the values into the vertical motion formula $h(t) = -16t^2 + vt + h_0$. Let $h(t) = 0$ b. Use the quadratic formula to find out how long the rocket will take to hit the ground after it is launched. Round to the nearest tenth of a second.